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Mecha	Mechanisms of Recrystallization in Superalloys			FA8655-06-M-4001			
			5h GR	ANT NUMBER			
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				Fo. DD	OGRAM ELEMENT NUMBER		
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Dr. Fra	ank J Montheillet						
				5d. TA	SK NUMBER		
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### **Center for Materials Science and Structures**

## Plasticity, Damage, and Corrosion of Materials CNRS Laboratory

# MECHANISMS OF RECRYSTALLIZATION IN SUPERALLOYS

EOARD Contract No. FA8655-06-M-4001

Final Report

F. Montheillet and J. Le Coze

January 2007

### Research Project No FA8655-06-M-4001

#### APPENDIX

- 1 The Contractor, Ecole des Mines de Saint-Etienne (ENSM-SE), hereby declares that, to the best of its knowledge and belief, the technical data delivered herewith under Contract No. FA8655-06-M-4001 is complete, accurate, and complies with all requirements of the contract.
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- 4 Disclosure of inventions: I certify that there were no subject inventions to declare during the performance of this grant.

Frank Montheillet
Directeur de Recherche au CNRS

### **CONTENTS**

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- IV. QUANTITATIVE ANALYSIS OF THE STRESS-STRAIN CURVES OF Ni-Nb ALLOYS
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- VI. DISCUSSION
- VII. CONCLUSIONS AND FUTURE DEVELOPMENTS

This work was carried out with the technical help of Mrs. Séverine Girard, Prisca Lévêque, Cécile Genevois, Marilyne Mondon, and Mr. Sébastien Saunier, who are gratefully acknowledged.

### I. INTRODUCTION

The general purpose of the present program is to investigate the mechanisms of dynamic recrystallization occurring during hot working of nickel base superalloys. More specifically, the role of niobium additions either as solute element or in the form of intermetallic precipitates is addressed. To discard interactions with other additions or impurities present in the industrial alloys, model materials prepared from pure nickel and niobium are used.

Former research, carried out under EOARD contract No. FA8655-03-M-4061, has shown that solid solution niobium has a strong influence on the hot deformation of nickel, for weight concentrations less than 1 % [Montheillet et al., 2006]. Since such effects appeared to increase very quickly between 0 and 1000 ppm (0.1wt%), a first natural step was to investigate an alloy with very low Nb content, *viz.* Ni-0.01 wt%Nb (referred to here as Ni-0.01Nb). Two other alloys containing 10 wt%Nb (Ni-10Nb) and 15 wt%Nb (Ni-15Nb), respectively, were prepared as well, as described in Section II.

Stress-strain curves of the two alloys Ni-0.01Nb and Ni-10Nb were investigated by torsion tests at various strain rates within the hot forging temperature range, which allow large strain steady state flow stresses to be reached. However, only a few data were obtained from the last alloy Ni-15Nb, due to its limited forgeability. The rheological behaviour of the alloys was then characterized by the classical strain rate sensitivity and apparent activation energy parameters (Section III).

In Section IV, the stress-strain curves of pure nickel and Ni-Nb alloys containing 0.01 %, 0.1 %, 1 %, and 10 %Nb (referred to as Ni-0.01Nb, Ni-0.1Nb, Ni-1Nb, and Ni-10Nb, respectively) are analyzed according to the Yoshie-Laasraoui-Jonas flow rule. The classical "Derby relationship" between the steady state average grain size and flow stress is investigated for the same model alloys in Section V.

Finally, the above data are discussed and compared in Section VI.

### II. PREPARATION OF MODEL HIGH PURITY BASE Ni-Nb ALLOYS

Three alloys were prepared using an induction melting device described elsewhere [Le Coze et al., 1995; Montheillet *et al.*, 2004]. Purification is performed by repeated melting under high purity argon-hydrogen atmosphere. The niobium and residual metalloid contents were measured by atomic absorption, spark emission spectroscopy, and inductive coupling plasma (optical emission spectroscopy, ICP-OES). The average results are given in Table I.

/S
1

Alloy	Nb (wt%)	C (ppm)	S (ppm)	O (ppm)	N (ppm)	Ni
Ni-0.01Nb	0.0105	5.5	5	4.5	1	Balance
Ni-10Nb	9.5	6	5	3.2	3	Balance
Ni-15Nb	15	4	4	9	4	Balance

Ingots of about 1.1 kg were hot forged at 1050 °C (furnace temperature) into cylindrical bars of diameter 16 mm and then reduced by swaging at the same temperature to a diameter of 10.7 mm. 13 torsion specimens of gauge length 27 mm and diameter 6 mm were then machined from each of the bars.

### III. RHEOLOGICAL BEHAVIOUR OF THE Ni-0.01Nb, Ni-10Nb, and Ni-15Nb ALLOYS

For comparison with previous data, large strain hot torsion tests were carried out at the same temperatures and strain rates, according to Table II, except for Ni-15Nb (see III.3). All specimens were heated to the test temperature up to stabilization ( $\approx 15 \, \text{min}$ ) and quenched using a room temperature flow of argon immediately after deformation to an outer strain of 5, where a steady state flow stress was clearly attained.

**Table II.** Temperature and strain rate conditions of the torsion tests carried out on pure Ni, Ni-0.01Nb, Ni-0.1Nb, Ni-1Nb, and Ni-10Nb

		Temperature (°C)				
		800 850 900 950 100				
Strain rate (s <sup>-1</sup> )	0.03	*		*		*
	0.10	*	*	*	*	*
	0.30	*		*		*

The above schedule was chosen to allow the determination of the strain rate sensitivity parameter at 800, 900, and 1000  $^{\circ}$ C and the apparent activation energy at 0.1 s<sup>-1</sup> with a good accuracy.

The "engineering" strain rate sensitivity  $\tilde{m} = \partial \ln \Gamma / \partial \ln \dot{N}$  was derived in a first step from the experimental data for N corresponding to the maximum torque ( $\tilde{m}_M$ ) and for the steady state ( $\tilde{m}_S$ ). Since the two values generally do not coincide and increase slightly with temperature, an overall average was used for deriving the flow stress according to the classical Fields and Backofen equation:

$$\sigma = \frac{\sqrt{3}\Gamma}{2\pi R_0^3} (3 + \tilde{m} + \tilde{n}) \tag{1}$$

where  $R_0$  is the outer radius of the specimen. In the above formula, the "engineering" strain hardening parameter  $\tilde{n} = \partial \ln \Gamma / \partial \ln N$  was determined in turn from each of the  $\Gamma - N$  curves using a smoothing and derivation procedure.

### III.1. Ni-0.01 Alloy

The stress-strain curves of alloy Ni-0.01Nb are displayed in the three diagrams of Figure 1 for strain rates of 0.03, 0.1, and 0.3 s<sup>-1</sup>, respectively. The overall shape of the curves is similar to that of pure nickel [Montheillet et al., 2006], but the flow stress is significantly higher. The oscillations following the peak flow stress are more visible than in Ni. In the latter case, these waves have been ascribed to possible artifacts, for instance the large initial grain size. In the present case, however, they could reflect grain size coarsening usually associated with multiple peak discontinuous dynamic recrystallization, although the initial grain size is likely to be quite large. This point should be checked in further work. Finally, the strain required to achieve flow stress steady state is larger than for pure nickel, which confirms that niobium solutes slows down the dynamic recrystallization process.

The strain rate sensitivity parameter m was determined at 800, 900 and 1000 °C for both the peak flow stress ( $m_M = \partial \ln \sigma_M / \partial \ln \dot{\epsilon}$ ) and the steady state flow stress ( $m_S = \partial \ln \sigma_S / \partial \ln \dot{\epsilon}$ ) from the  $\log \sigma - \log \dot{\epsilon}$  curves of Figure 2. Data reported in Table III show that m slightly increases with temperature, with average values  $m_M = 0.173$  and  $m_S = 0.134$  (very close to their "engineering" counterparts,  $\tilde{m}_M$  and  $\tilde{m}_S$ , respectively). It is worth to note that  $m_S$  is significantly lower than  $m_M$ .

The apparent activation energy for deformation of the alloy was determined in turn for the peak flow stress  $(Q_M)$  and the steady state flow stress  $(Q_S)$  at a strain rate of  $0.1~s^{-1}$  from the  $\ln\sigma-1/T$  plot of Figure 3. As it was already noticed for Ni and the alloys Ni-0.1Nb and Ni-1Nb, the five available points are remarkably aligned in this diagram [Montheillet et al., 2006]. Since the slope of the curve is  $\partial\ln\sigma/\partial(1/T)=mQ/R$ , where R is the gas constant, this means that the *product* mQ is independent of temperature. Using the above averages  $m_M$  and  $m_S$ , the following values were obtained:  $Q_M=253~kJ/mol$  and  $Q_S=310~kJ/mol$ .

Table III. Strain rate sensitivity values of the Ni-0.01Nb alloy

Temperature (°C)	m <sub>M</sub> (peak stress)	m <sub>S</sub> (steady state stress)
800	0.163	0.114
900	0.190	0.142
1000	0.165	0.145
Average	0.173	0.134

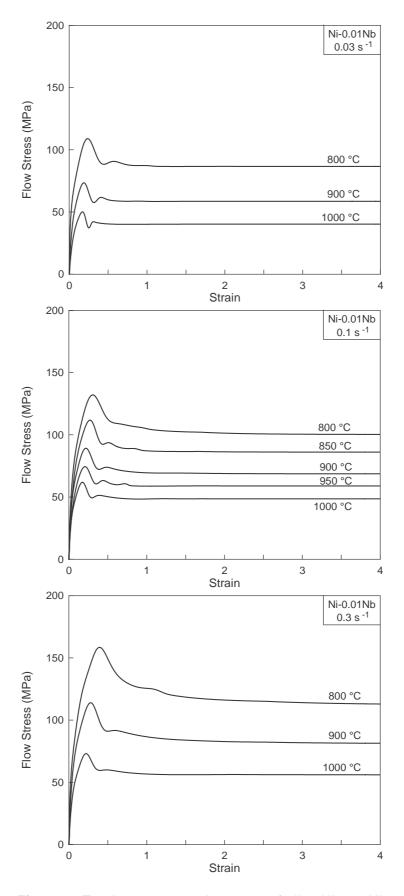
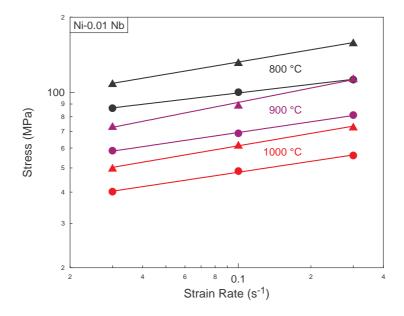
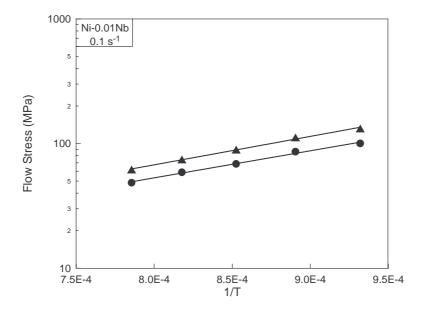


Figure 1. Torsion stress-strain curves of alloy Ni-0.01Nb



**Figure 2.** Strain rate dependence of the flow stress of alloy Ni-0.01Nb (triangles: peak stress; circles: steady state stress)



**Figure 3.** Temperature dependence of the flow stress of alloy Ni-0.01Nb (triangles: peak stress; circles: steady state stress)

### III.2. Ni-10Nb Alloy

According to the Ni-Nb phase diagram (see Figure 7), niobium remains entirely in solid solution within the investigated temperature range. As expected, the flow stress level is much higher than for pure nickel or even Ni-1Nb (Figure 4). For instance, at 800 °C and 0.1 s<sup>-1</sup>, the peak flow stress  $\sigma_{\rm M}$ = 105 MPa for Ni, 282 MPa for Ni-1Nb and 586 MPa for Ni-10Nb. For that reason, the three flow curves at 800 °C, as well as that at 900 °C-0.3 s<sup>-1</sup>, are significantly affected by self-heating (fracture of the specimen has even occurred before the end of the test in two cases). Under such straining conditions, only the peak flow stress was therefore considered.

The double logarithmic stress-strain rate plot is shown in Figure 5. The associated values of the strain rate sensitivity parameters  $m_M$  (peak stress) and  $m_S$  (steady state stress) are reported in Table IV. It is worth to note that  $m_M$  increases strongly with temperature, while for  $m_S$  the trend is not obvious.

The  $\ln \sigma - 1/T$  plots at  $\dot{\epsilon} = 0.1 \text{ s}^{-1}$  are shown in Figure 6. Like in the previous cases, the point data are remarkably aligned for both  $\sigma_M$  and  $\sigma_S$ . This means again that the *products*  $m_M Q_M$  and  $m_S Q_S$  are constant (*i.e.* independent of temperature). A consequence is that  $Q_M$  strongly decreases with increasing temperature (Table IV).

**Table IV.** Strain rate sensitivity and apparent activation energy (at 0.1 s<sup>-1</sup>) values for the peak stress ( $m_M$ ,  $Q_M$ ) and the steady state flow stress ( $m_S$ ,  $Q_S$ ) of the Ni-10Nb alloy

Temperature (°C)	$m_{\mathrm{M}}\mathrm{Q}_{\mathrm{M}}/\mathrm{R}$ $(\mathrm{K})$	$m_{\mathrm{M}}$	Q <sub>M</sub> (kJ/mol)	$m_{\rm S}Q_{\rm S}/R$ (K)	m <sub>S</sub>	Q <sub>S</sub> (kJ/mol)
800		0.050	977		-	-
900	5872	0.127	385	5069	0.118	357
1000		0.179	273		0.111	380

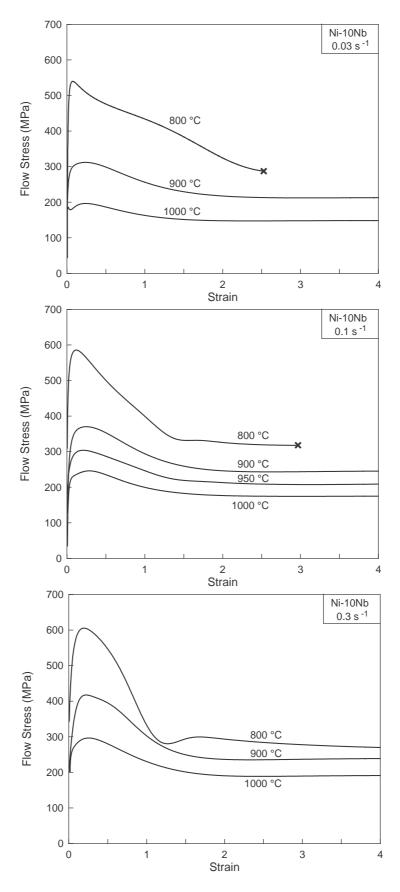
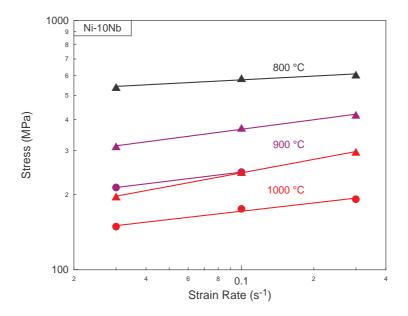
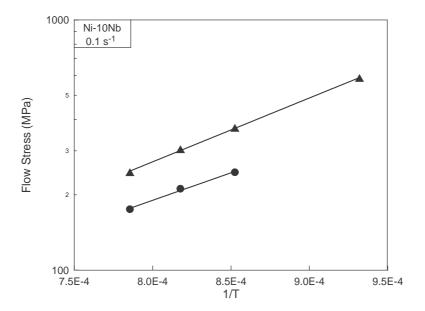


Figure 4. Torsion stress-strain curves of alloy Ni-10Nb (crosses mean fracture)



**Figure 5.** Strain rate dependence of the flow stress of alloy Ni-10Nb (triangles: peak stress; circles: steady state stress)



**Figure 6.** Temperature dependence of the flow stress of alloy Ni-10Nb (triangles: peak stress; circles: steady state stress)

### III.3. Ni-15Nb Alloy

The last alloy Ni-15Nb was initially prepared to compare the influence of niobium in solid solution and in the form of intermetallic precipitates (Ni<sub>3</sub>Nb) on the hot working behaviour. Since the atomic fraction of niobium is close to 10 %, the phase diagram in Figure 7 shows that precipitation is likely to occur (in static conditions) below 1000 °C. Solid solution annealing for 15 min at 1050 °C was therefore carried out on the specimens, which were then cooled to the deformation temperature. Torsion test were then performed (i) after 10 min holding at the deformation temperature, assuming that no precipitation would take place during this interval; (ii) after 2 h holding in order to produce Ni<sub>3</sub>Nb precipitation (see dilatometry data in Section VI.3). Unfortunately, due to the high stress level associated with self-heating, most of the specimens broke at strains less than the scheduled  $\varepsilon = 5$  and before a steady state flow stress was reached (Figure 8).

For the above reasons, it was not possible to determine the rheological parameters of this alloy. However, the apparent activation energy can be estimated from the observation that the (steady state) flow stresses are very close in the two straining conditions 900 °C - 0.005 s<sup>-1</sup> and 1000 °C - 0.1 s<sup>-1</sup>: identification of the associated Zener-Hollomon parameters leads to  $Q \approx 372$  kJ/mol.

The behaviour of this alloy will be discussed below (Section VI) from dilatometry measurements, X-ray diffraction, and electron microscopy observations.

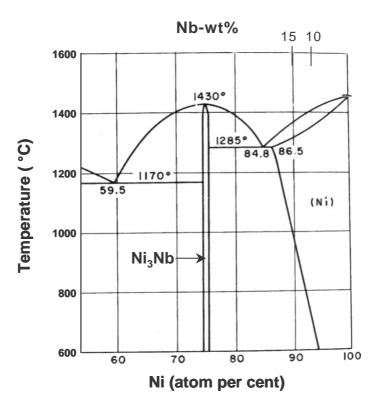


Figure 7. Ni rich part of the Ni-Nb phase diagram

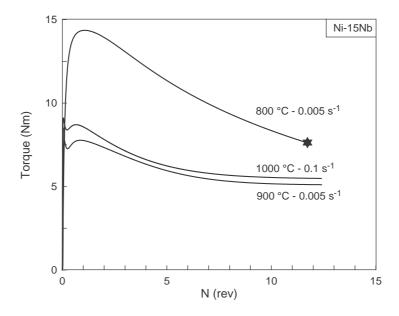


Figure 8. Torque-twist curves of alloy Ni-15Nb (the star means fracture)

### IV. QUANTITATIVE ANALYSIS OF THE STRESS-STRAIN CURVES OF Ni-Nb ALLOYS

In this section, the flow curves pertaining to the pure nickel, and alloys Ni-0.01Nb, Ni-0.1Nb, Ni-1Nb, Ni-10Nb are analyzed using the Yoshie-Laasraoui-Jonas (YLJ) flow rule [Yoshie et al., 1987; Laasraoui and Jonas, 1991]. The latter accounts for strain hardening and dynamic recovery, starting from the microscopic equation:

$$\frac{\mathrm{d}\rho}{\mathrm{d}\varepsilon} = \mathbf{h} - \mathbf{r}\,\rho\tag{2}$$

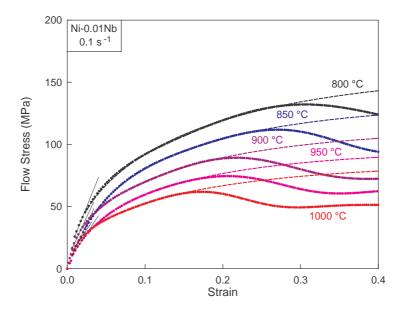
where  $\rho$  is the dislocation density, h the strain hardening parameter and r the dynamic recovery parameter. Integration of eq. (2) and combination with the classical relationship  $\sigma = \alpha \mu \, b \sqrt{\rho}$ , where  $\alpha \approx 1$ ,  $\mu$  is the elastic shear modulus and b the Burgers vector modulus, lead to:

$$\sigma = \left\{ \sigma_{\infty}^2 - (\sigma_{\infty}^2 - \sigma_{e}^2) \exp\left[-r(\varepsilon - \varepsilon_{e})\right] \right\}^{1/2}$$
 (3)

Here  $\epsilon_e$  and  $\sigma_e$  denote the coordinates of a conventional yield point, and  $\sigma_\infty = \alpha \mu b \sqrt{h/r}$  is the (virtual) steady state stress level, that would be achieved in the absence of dynamic recrystallization.

For each stress-strain curve, the yield point  $(\epsilon_e, \sigma_e)$  was determined empirically. A numerical procedure was then employed to derive the values of r and  $\sigma_\infty$  giving the best fit of equation (3) with the data. Since dynamic recrystallization is expected to start somewhere before the peak flow stress  $(\epsilon = \epsilon_M)$ , only data points for

 $\varepsilon < (5/6)\varepsilon_{\rm M}$  were taken into consideration [Rossard, 1973]. Figure 9 shows a typical example of the results in the case of Ni-0.01Nb deformed at 0.1 s<sup>-1</sup>. In all cases, the agreement between the data and the YLJ equation is quite good.



**Figure 9.** Example showing how the YLJ equation (broken lines) fits the first part (*i.e.*, before the onset of DRX) of the experimental stress-strain curves (dotted lines)

### IV.1. Determination of $\sigma_{\infty}$ and r

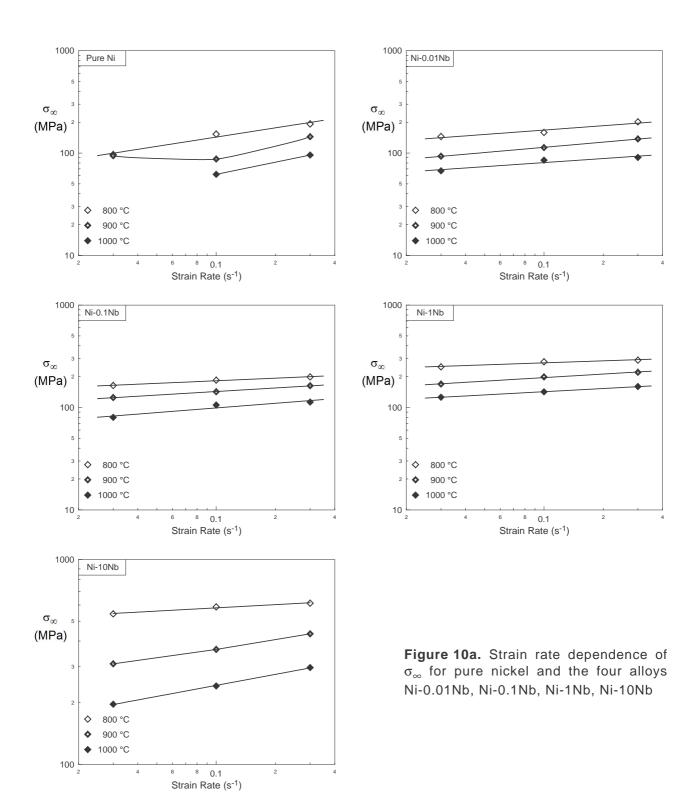
In a first step, each flow curve was associated with the values of r and  $\sigma_{\infty}$  and the strain rate and temperature dependence of these two parameters was then investigated for the various materials. According to former investigations [Montheillet, 2004], such dependence is expected to be of the form:

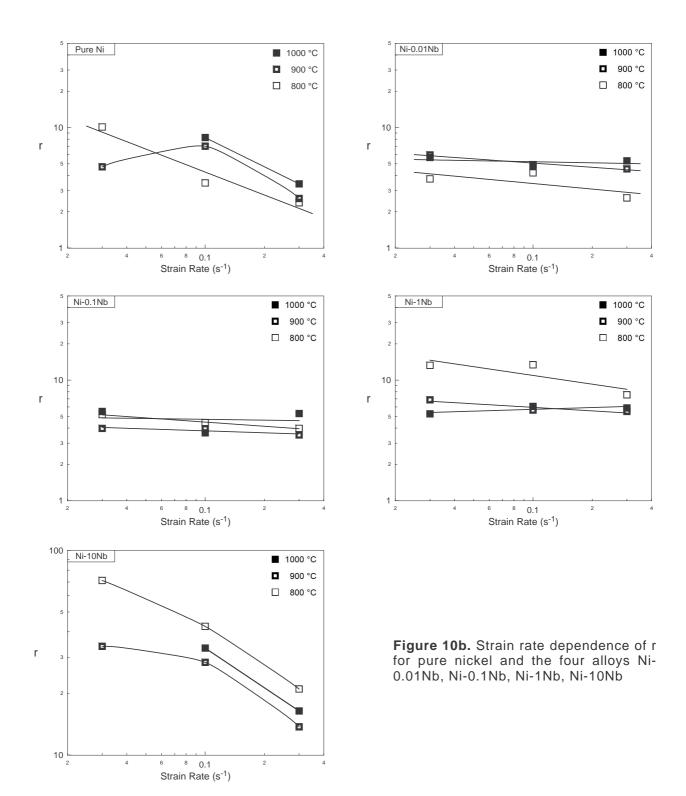
$$\sigma_{\infty} = B \dot{\varepsilon}^{m_{\infty}} \exp\left(\frac{m_{\infty} Q_{\infty}}{RT}\right) \tag{4}$$

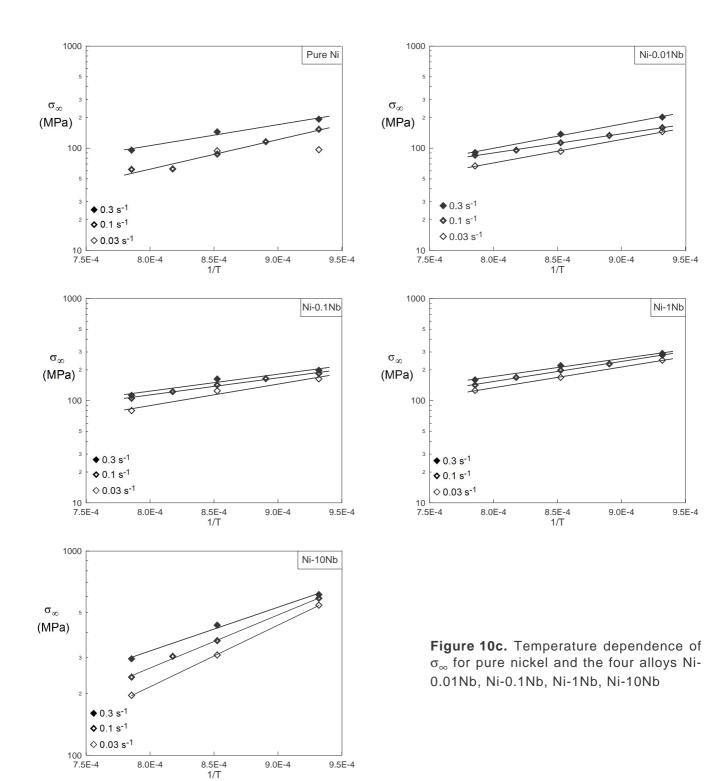
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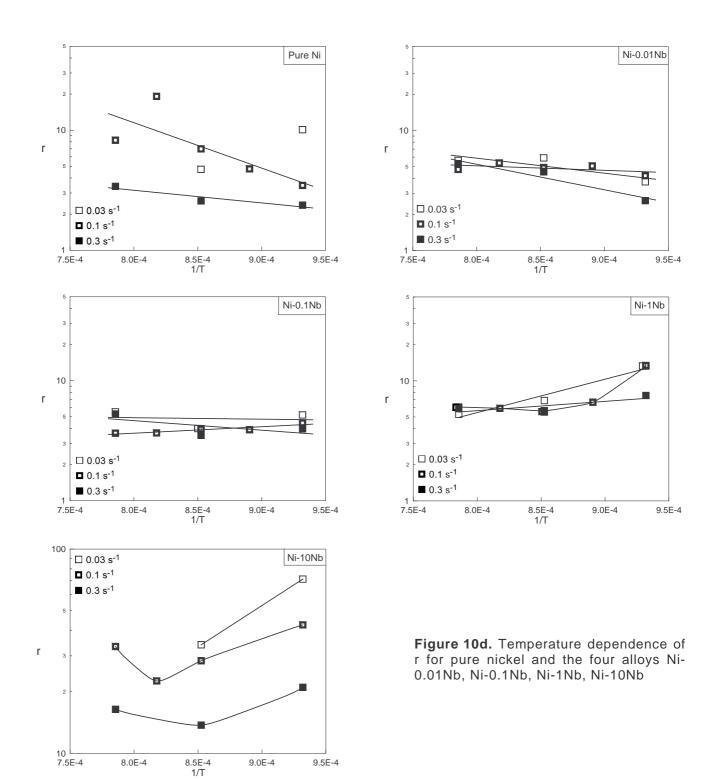
$$r = r_0 \,\dot{\varepsilon}^{-m_r} \exp\left(-\frac{m_r Q_r}{RT}\right) \tag{5}$$

where  $m_{\infty}$ ,  $m_r$  and  $Q_{\infty}$ ,  $Q_r$  are the strain rate sensitivities and apparent activation energies associated with  $\sigma_{\infty}$  and r, respectively, and R is the gas constant. The results are plotted in Figures 10a-d for pure nickel and the four alloys Ni-0.01Nb, Ni-1Nb, Ni-1Nb, Ni-10Nb.









The first comments are the following:

a) Strain rate sensitivities: Figure 10a shows that the assumption of a power law relationship dependence of  $\sigma_{\infty}$  [eq.(4)] is quite correct and the corresponding  $m_{\infty}$  are reported in Table V. The average  $m_{\infty}$  decreases with the addition of niobium. For r, there is more scattering of the data (Figure 10b). However,  $m_r$  seems also to drop with an increasing niobium content; for the Ni-0.1Nb, and Ni-1Nb alloys,  $m_r$  is quite low, especially at 1000 °C.

**Table V.** Strain rate sensitivities  $m_{\infty}$  and  $m_r$  associated with  $\sigma_{\infty}$  and r, respectively (brackets indicate estimated values)

	T (°C)	$\mathrm{m}_{\infty}$	m <sub>r</sub>
	800	0.300	0.633
Ni	900	[0.458]	-
	1000	[0.395]	0.805
	800	0.142	0.154
Ni-0.01Nb	900	0.169	0.117
	1000	0.132	0.030
	800	0.084	0.115
Ni-0.1Nb	900	0.115	0.054
	1000	0.151	0.023
	800	0.066	0.241
Ni-1Nb	900	0.115	0.097
	1000	0.104	- 0.050
	800	0.052	
Ni-10Nb	900	0.146	-
	1000	0.179	

b) Temperature sensitivities: For  $\sigma_{\infty}$ , the point data are remarkably aligned (Figure 10c), which supports the Arrhenius form of eq.(4). The values of the slope  $\overline{m}_{\infty}Q_{\infty}/R$  and the associated apparent activation energies  $Q_{\infty}$  are reported in Table VI. Here  $\overline{m}_{\infty}$  denotes the average value of  $m_{\infty}$  over the investigated temperature range, that was used to derive  $Q_{\infty}$ . At 0.03 and 0.1 s<sup>-1</sup>, niobium addition seems to significantly increase  $Q_{\infty}$ . However, this trend is not verified at 0.3 s<sup>-1</sup>, which could be due to self-heating during the tests. For r, the data are again more scattered, but  $\overline{m}_rQ_r$  (where  $\overline{m}_r$  is the averaged  $m_r$  value) globally decays with increasing niobium content, to become close to zero or even negative in Ni-0.1Nb and Ni-1Nb (Figure 10d). Furthermore,  $m_r$  is low for these two alloys. It is worth to note that whenever  $m_r = 0$ , it is not possible to derive any  $Q_r$ , which is tantamount to say that the argument  $m_rQ_r$  of the exponential in eq.(4) is not relevant in such a case. For the last alloy Ni-1Nb, the variations of  $\overline{m}_rQ_r$  are not monotonic over the investigated temperature range, such that  $Q_r$  was not determined.

### IV.2. Determination of h

The strain hardening parameter h was determined in a second step from its definition:

$$\sigma_{\infty} = \alpha \mu b \sqrt{h/r} \tag{6}$$

where  $\alpha$  was assumed to equal unity, and  $b = 2.49 \times 10^{-10}$  m (pure nickel). The elastic shear modulus  $\mu$  was in turn determined as a function of temperature from the following equation [Frost and Ashby, 1982]:

$$\mu = \mu_0 \left( 1 + \eta \frac{T - 300}{T_M} \right) \tag{7}$$

with, to a first approximation,  $\mu_0 = 7.89 \times 10^4$  MPa (for Ni at 300 K),  $T_M = 1726$  K (Ni), and  $\eta = -0.64$ .

The values are displayed in Figure 11 in an h-r diagram for comparison of the five materials investigated. It is interesting to note that r is ranging roughly between 2 and 10 for pure nickel and the low alloy materials (up to 1 %Nb), which is to be compared with the value  $r \approx 5$  recently found for a model alloy close to 304 stainless steel [Gavard, 2001]. Such low value is likely to reflect the weak recovery capacity of low stacking fault energy materials. By contrast, Ni-1Nb displays much higher r-values. However, the latter are not likely to reflect a more efficient dynamic recovery in this alloy, but rather the fact that the flow stress level is partly governed by solute drag, instead of dislocation density. Figure 11 also shows that the strain hardening parameter h is not sensitive to niobium solutes up to 0.1 %, but increases significantly for Ni-1Nb and Ni-10Nb.

Table VI. Temperature dependence parameters associated with  $\sigma_{\infty}$  and r (brackets indicate estimated values)

	$\dot{\epsilon}(s^{-1})$	$\overline{m}_{\infty}Q_{\infty}/R$ (K)	$Q_{\infty}$ (kJ/mol)	$\overline{m}_r Q_r / R$ (K)	Q <sub>r</sub> (kJ/mol)
	0.03	-	-	-	
Ni	0.1	6654	[144]	8706	101
	0.3	4730	[102]	2423	28
	0.03	5275	297	2880	239
Ni-0.01Nb	0.1	4312	243	861	71
	0.3	5440	307	4898	406
	0.03	4845	346	287	37
Ni-0.1Nb	0.1	3836	274	- 1246	- 162
	0.3	3816	272	1826	237
	0.03	4667	409	- 6394	- 554
Ni-1Nb	0.1	4517	396	-	-
	0.3	4035	353	- 1782	- 154
	0.03	6941	460		
Ni-10Nb	0.1	5975	396		
	0.3	4922	326		

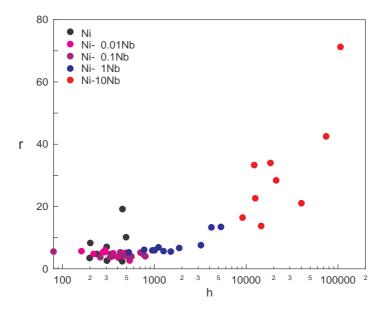


Figure 11. Diagram showing the h and r values of the five materials investigated

### IV. STEADY STATE STRESS VS. GRAIN SIZE RELATIONSHIP

A number of authors have found an inverse power law relationship between the steady state flow stress and the average steady state grain (or crystallite) size:

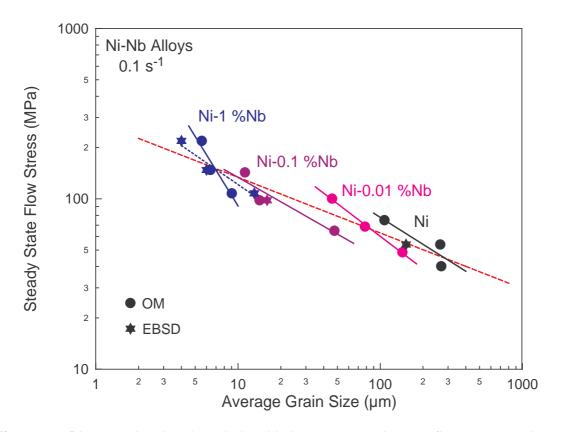
$$\sigma_{s} = K / \overline{D}^{a} \tag{8}$$

with an exponent a generally ranging between 0.6 and 0.8 [Derby, 1992].

Metallographic observations were carried out on the four grades Ni, Ni-0.01Nb, Ni-0.1Nb, and Ni-1Nb deformed to a strain of 5 ( $\approx$  steady state) at the three temperatures 800, 900, and 900 °C for  $\dot{\epsilon} = 0.1 \, \text{s}^{-1}$ . Metallographic preparation of the specimens involved mechanical polishing up to 3  $\mu m$ , electrolytic polishing, and chemical etching (CuCl<sub>2</sub> solution). A quantitative analysis software was used to determine the mean equivalent circle diameter (ECD) of the grains, considered here to be representative of the average grain size.

The results are displayed in Figure 12, together with some EBSD data points obtained previously (in the latter case, the grain size was identified to the mean intercept of boundaries associated with a misorientation angle larger than 15 deg). The values of the exponent a are reported in Table VII. For Ni and the alloys Ni-0.01Nb and Ni-0.1Nb, a is slightly less than usually reported, while the value a = 1.35 for Ni-1Nb (optical microscopy) is much larger. However, EBSD data lead to a = 0.58 for the same alloy, which seems to be more reliable. Unexpectedly, the diagram shows that for a given grain size, the flow stress *decreases* with increasing niobium content. This suggests that the hardening effect of niobium in solid solution is basically related to grain refinement. Finally, it is worth to note that when the (OM) data pertaining to the various materials are considered together (broken line), a

takes the value 0.33, which is quite smaller than that obtained by Derby [1992], who considered a set of data relative to various industrial alloys.



**Figure 12.** Diagram showing the relationship between steady state flow stress and average grain size. Optical microscopy (OM) and EBSD data. The broken line fits the whole set of OM data.

**Table VII.** Exponent a of the steady state flow stress *vs.* grain size relationship (OM: optical microscopy)

	a
Ni (OM)	0.53
Ni-0.01Nb (OM)	0.64
Ni-0.1Nb (OM)	0.48
Ni-1Nb (OM)	1.35
Ni-1Nb (EBSD)	0.58
All OM data	0.33

### VI. DISCUSSION

Putting together the above results and that previously obtained [Montheillet et al., 2004] allows the influence of niobium solutes on the hot deformation of nickel to be analyzed.

### VI.1. Solid solution hardening

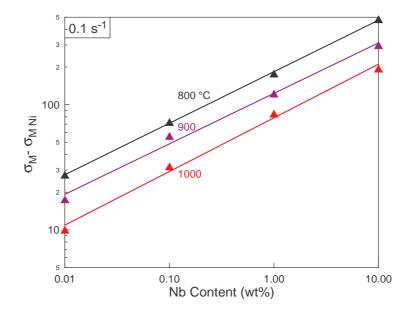
Both the peak flow stress  $\sigma_M$  and the steady state flow stress  $\sigma_S$  increase very rapidly with the niobium content, as illustrated by Figure 13 for pure nickel and the four Ni-Nb alloys. In spite of data scattering, the following power law dependence of the flow stress is confirmed:

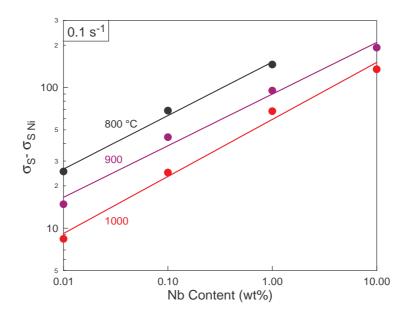
$$\sigma = \sigma_0 + k x^p \tag{9}$$

where x is the solute content (wt%) and p ranges from 0.37 to 0.43. Such hardening law is different from the classical linear dependence frequently reported in the literature (for larger solute contents) at room temperature. It should be kept in mind, however, that hot deformation is addressed here and that  $\sigma_M$  and  $\sigma_S$  are likely to be influenced by the initial grain size and the steady state grain size, respectively. Both are expected to decrease with increasing x, and therefore contribute to hardening. In fact, it has been shown in the previous section that the flow stress hardening by niobium in nickel is due to grain refinement rather than to direct solute effects.

### VI.2. Strain rate and temperature dependence of the flow stress

Figure 14 shows the influence of niobium concentration on the product mQ, and the classical rheological parameters m and Q considered separately. The product mQ clearly goes through a maximum at low niobium concentrations, but increases again for Ni-10Nb. By contrast, m and Q are monotonic decreasing and increasing functions of the niobium content, respectively, although the trend is not exactly confirmed for Ni-10Nb. The influence of niobium is strong but appears to become much less efficient at concentrations larger than 0.1 wt%. These observations suggest that the mechanism controlling the flow stress level is not the same at low (< 0.1 %) and large ( $\geq$  10 %) niobium concentrations.





**Figure 13.** Influence of niobium content on the peak and steady state flow stresses of pure nickel and the Ni-Nb alloys at various temperatures and a strain rate of  $0.1 \, \text{s}^{-1}$ 

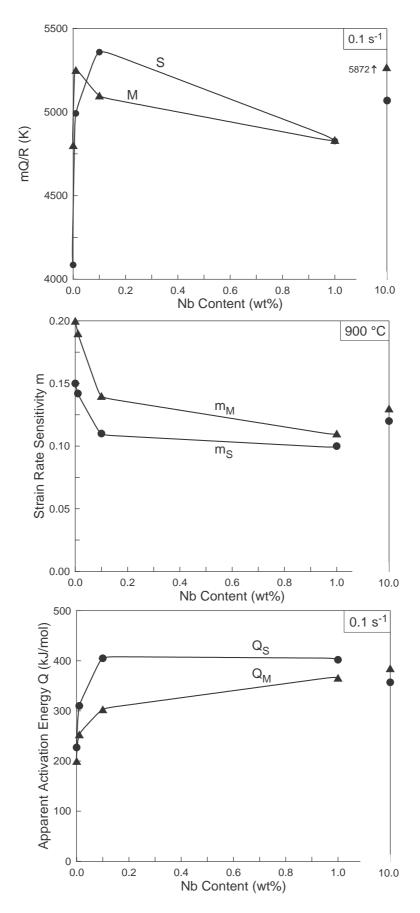


Figure 14. Influence of the solute niobium content on mQ, m and Q (M: peak stress; S: steady state stress)

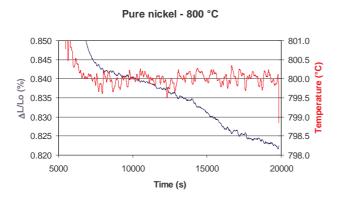
### VI.3. Behaviour of the Ni-15Nb alloy

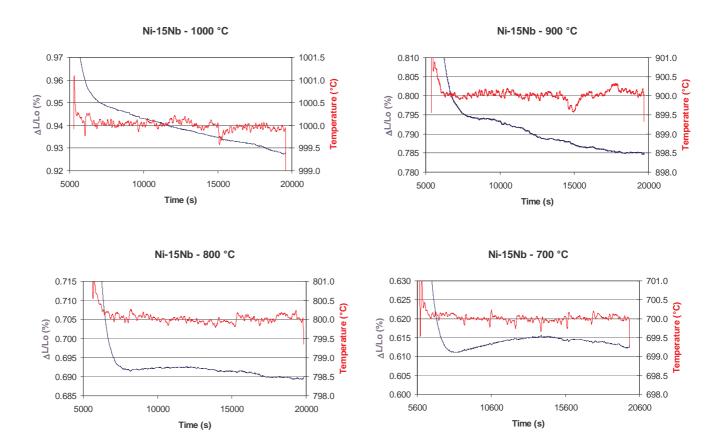
Three types of observation were used to check if intermetallic precipitates were present before and/or after deformation in the alloy Ni-15Nb (see Section III.3 above). First, dilatometry measurements were carried out on pure nickel at 800 °C, and on the Ni-15Nb alloy at 1000, 900, 800, and 700 °C. In each case, the specimen was first annealed for 1 h at 1050 °C to ensure complete dissolution of niobium precipitates, and then slowly cooled to the selected temperature. Isothermal length changes of the specimen were then recorded. Figure 15 exhibits monotonic contractions for Ni-15Nb at 1000 °C and 900 °C, as well as for pure nickel at 800 °C. By contrast, for Ni-15Nb at 800 °C and 700 °C, the inverse trend is observed after about 25 min holding at the test temperature (after the cooling time). Such behaviour is likely to reflect intermetallic precipitation, in agreement with the phase diagram of Figure 7. Furthermore, at given temperature, the latter appears to be much slower than in industrial alloys.

X-ray diffraction measurements were then performed on specimens of Ni-15Nb after various holding times at 800 °C (15 min and 120 min) and 900 °C (10 min), as well as on a torsion specimen strained to  $\varepsilon = 5$  at 900 °C and  $5 \times 10^{-3} \, \mathrm{s}^{-1}$ . In all cases, there was no evidence of precipitation. Furthermore, the lattice parameter was close to 0.359 nm, which corresponds to a Ni-Nb solid solution containing about 10 at%Nb [Pearson, 1964].

Finally, transmission electron microscopy observations were carried out on the same specimens as above. In all cases, diffraction patterns exhibited only spots associated with the nickel matrix, and no precipitates could be identified on the bright field images.

It can therefore be concluded that if intermetallic precipitates ( $Ni_3Nb$ ) are present in the Ni-15Nb alloy, they must be ultrafine. Their volume fraction is likely to be low, since the matrix parameter indicates a solute content close to 10 at%. Furthermore, dilatometric measurements show that, if precipitation really occurs, its kinetics must be quite slow.





**Figure 15.** Dilatometry measurements carried out on pure nickel at 800 °C and on alloy Ni-15Nb at 1000, 900, 800, and 700 °C

### V. CONCLUSIONS AND FUTURE DEVELOPMENTS

The results reported above have to be combined with that presented in a previous report [Montheillet et al., 2004]. They contribute to the knowledge of the influence of niobium (mostly in solid solution) during hot working of Ni base alloys:

(i) Niobium solutes increase the peak and steady state flow stresses quite efficiently according to a power law relationship  $\sigma = \sigma_0 + k x^p$ , where x is the niobium content (wt%) and p is close to 0.4.

Such effect, however, is apparent, in the sense that the flow stress level also depends on the initial and steady state grain sizes, respectively. In particular, in the case of the steady state flow stress, it has been shown that the hardening effect of niobium solutes is *indirect*, since it is entirely due to grain size refinement.

- (ii) For all materials, the  $\ln \sigma (1/T)$  plots are perfectly linear, which means that the product mQ is independent of temperature, although m and Q taken separately are not. Niobium solutes decrease the strain rate sensitivity of the flow stress and increase the apparent activation energy. Such effects are quite strong for low (< 0.1 wt%) niobium contents but saturate at larger concentrations.
- (iii) A quantitative analysis of the flow rules using the Yoshie-Laasraoui-Jonas equation led to the determination of the rheological parameters  $\sigma_{\infty}$ , h and r. The first one denotes the steady state flow stress in the absence of dynamic recrystallization, whereas h depicts the kinetics of strain hardening, and r the kinetics of dynamic recovery (for low alloy materials). These parameters allow to quantify the material behaviour, and can be used to analyze the effect of niobium on the various elementary mechanisms of hot deformation. In particular, they are likely to reflect the possible change of controlling mechanism with increasing niobium content.
- (iv) Finally, it was shown that intermetallic precipitation in the Ni-15Nb alloy -if it occurs- should be very fine and associated with slow kinetics. Since it was not possible to determine the rheological parameters of this alloy, the question of the influence of precipitation on the hot working behaviour is still open. However, the present data show that binary Ni-Nb alloys are good model materials for such investigations, since Ni<sub>3</sub>Nb precipitation is much slower than in industrial alloys such as IN 718.

Short-term developments of this research would aim at completing our knowledge of the hot working behaviour and mechanisms of the binary Ni-Nb alloys. This would include a more detailed investigation of the respective influences of niobium solutes and grain size (*i.e.*, initial or resulting from dynamic recrystallization) on the flow stress levels and the associated rheological parameters. For that purpose, new optical metallography and EBSD observations should be carried out on the deformed specimens of the various alloys. It would also be useful to investigate the deformation textures, that are likely to influence the steady state flow stress.

Since the results obtained on binary Ni-Nb alloys were partly unexpected, it would be interesting, as longer-term perspective, to analyze the hot working

behaviour of a model material closer to the classical nickel base superalloys (such as IN 718), starting from a Ni-Cr or Ni-Cr-Fe base with controlled additions of niobium

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